

$$PE_{\max} = KE_{\max}$$

$$mgh = \frac{1}{2}mv^2$$

Work-Energy Calculations

Study Lesson 2 of the Work, Energy and Power chapter at The Physics Classroom:

<http://www.physicsclassroom.com/Class/energy/u5l2bc.html>

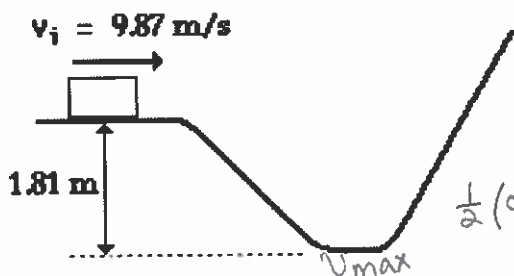
For the following questions, begin with the work-energy equation, cancel terms, substitute and solve.

1. A glider is gliding through the air at a height of 416 meters with a speed of 45.2 m/s. The glider dives to a height of 278 meters. Determine the glider's new speed.

$$KE_i + PE_i + \cancel{W_{\text{ext}}} = KE_f + PE_f$$

$$\frac{1}{2}(45.2 \text{ m/s})^2 + (9.8)(416 \text{ m}) = \frac{1}{2}(v^2) + (9.8)(278 \text{ m})$$

$$v = 68.9 \text{ m/s}$$



2. A box with mass m is sliding along on a friction-free surface at 9.87 m/s at a height of 1.81 m. It travels down the hill and then up another hill.
a. Find the speed at the bottom of the hill.

$$KE_i + PE_i + \cancel{W_{\text{ext}}} = KE_f + \cancel{PE_f}$$

$$\frac{1}{2}(9.87 \text{ m/s})^2 + (9.8)(1.81 \text{ m}) = \frac{1}{2}(v^2) + (9.8)(0 \text{ m})$$

$$v = 11.6 \text{ m/s}$$

- b. Find the maximum vertical height to which the box will rise on the opposite hill.

$$\cancel{KE}_i^{\max} + PE_i + \cancel{W_{\text{ext}}} = \cancel{KE}_f + PE_f^{\max}$$

$$\frac{1}{2}(11.6 \text{ m/s})^2 = (9.8)(h)$$

$$h = 6.88 \text{ m}$$

3. A 1423-kg car is moving along a level highway with a speed of 26.4 m/s. The driver takes the foot off the accelerator and the car experiences a retarding force of 901-N over a distance of 106 m. Determine the speed of the car after traveling this distance.

$$\cancel{KE}_i + \cancel{PE}_i + \cancel{W_{\text{ext}}} = KE_f + \cancel{PE}_f$$

$$\frac{1}{2}(1423 \text{ kg})(26.4 \text{ m/s})^2 + -(901 \text{ N} \cdot 106 \text{ m}) = \frac{1}{2}(1423 \text{ kg})v^2$$

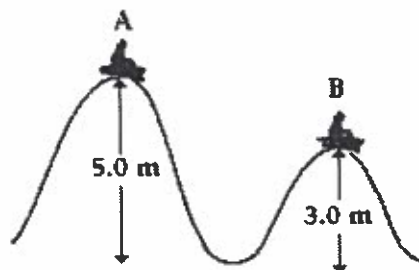
$$v = 23.7 \text{ m/s}$$

4. A sledder starts from rest atop a 5.0-m high hill (A). She sleds to the bottom and up to the top of the adjacent 3.0-m high hill. How fast is the sledder going at point B? Ignore friction.

$$\cancel{KE}_i + PE_i + \cancel{W_{\text{ext}}} = KE_f + PE_f$$

$$(9.8)(5.0 \text{ m}) = \frac{1}{2}(v^2) + (9.8)(3.0 \text{ m})$$

$$v = 6.3 \text{ m/s}$$



Work, Energy, and Power

5. A 4768-kg roller coaster train full of riders approaches the loading dock at a speed of 17.1 m/s. It is abruptly decelerated to a speed of 2.2 m/s over a distance of 13.6 m. Determine the retarding force that acts upon the roller coaster cars.

$$\cancel{KE_i} + \cancel{PE_i} + W_{ext} = \cancel{KE_f} + \cancel{PE_f}$$

$$\frac{1}{2}(4768 \text{ kg})(17.1 \text{ m/s})^2 - F(13.6 \text{ m}) = \frac{1}{2}(4768 \text{ kg})(2.2 \text{ m/s})^2$$

$$F =$$

6. A catcher's mitt recoils a distance of 12.9 cm in bringing a 142-gram baseball to a stop. If the applied force is 588 N, then what was the speed of the baseball at the moment of contact with the catcher's mitt?

$$\cancel{KE_i} + \cancel{PE_i} + W_{ext} = \cancel{KE_f} + \cancel{PE_f}$$

$$\frac{1}{2}(.142 \text{ kg})(v^2) - (588 \text{ N})(.129 \text{ m}) = 0 \text{ J}$$

$$v = 32.7 \text{ m/s}$$

7. An unknown force is applied to a 12 kg mass. The force acts at an angle of 30 degrees above the horizontal. Determine the force acting if the force acts for a horizontal displacement of 22 meters and increases the 12 kg mass's speed from 11 m/s to 26 m/s.

$$\cancel{KE_i} + \cancel{PE_i} + W_{ext} = \cancel{KE_f} + \cancel{PE_f}$$

8. A physics teacher exerts a force upon a 3.29-kg pile of snow to both lift it and set it into motion. The snow leaves the shovel with a speed of 2.94 m/s at a height of 0.562 m. Determine the work done upon the pile of snow.

$$\cancel{KE_i} + \cancel{PE_i} + W_{ext} = \cancel{KE_f} + \cancel{PE_f}$$

$$W = \frac{1}{2}(3.29 \text{ kg})(2.94 \text{ m/s})^2 + (3.29 \text{ kg})(9.8)(.562 \text{ m})$$

$$W = 32.3 \text{ J}$$

9. A 250.-gram cart starts from rest and rolls down an inclined plane from a height of 0.541 m. Determine its speed at a height of 0.127 m above the bottom of the incline.

$$\cancel{KE_i} + \cancel{PE_i} + \cancel{W_{ext}} = \cancel{KE_f} + \cancel{PE_f}$$

$$(.250 \text{ kg})(9.8)(.541 \text{ m}) = \frac{1}{2}(.250 \text{ kg})(v^2) + (.250 \text{ kg})(9.8)(.127 \text{ m})$$

$$v = 2.85 \text{ m/s}$$

10. A 4357-kg roller coaster car starts from rest at the top of a 36.5-m high track. Determine the speed of the car at the top of a loop that is 10.8 m high.

$$\cancel{KE_i} + \cancel{PE_i} + \cancel{W_{ext}} = \cancel{KE_f} + \cancel{PE_f}$$

$$(4357 \text{ kg})(9.8)(36.5 \text{ m}) = \frac{1}{2}(4357 \text{ kg})(v^2) + (4357 \text{ kg})(9.8)(10.8 \text{ m})$$

$$v = 22.4 \text{ m/s}$$